

Lecture 3 – Sampled Images

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Notes not for display – for notes only

Overview

- Last Time
 - Light -> Images
 - Sensing on the Image plane
 - Eyes
 - Unanswered questions
 - Interlace
 - What does it mean to have a sampled representation?
- Today
- Intensity, Quantization, Gamma Correction
 - Image Representation
 - Sampling for imaging
 - Sampling for display
 - Issues in Sampling
 - Aliasing
 - Sampling, Reconstruction, Resampling, Aliasing

The image plane

- 2D (surface, even if not flat)
- Distribution of light – can measure anywhere
 - $F(x,y)$
- Discrete set of points
 - Measurements taken
 - Measurements displayed
- Represent this discrete set of measurements
 - Regular “lattice” of measurements
 - Often a grid

How sensitive is the eye?

- Amazing range!
 - Night vision – when eyes adjusted, camping
 - Bright daylight
 - Sunlight 10000.
 - Twilight 10.
 - Starlight 0.001
- Catch: at any given time, can't see this range
 - Adaptation – bright light, iris closes, lets in less light, ...
- At any given time, about 100:1 contrast ratio
 - This is a lot more than most displays
 - Better displays = more contrast
 - Often by blacker blacks

High Dynamic Range Imagery

- Most sensors/displays have less range than eye
 - Certainly less range than scenes do
- What happens?
 - Bright areas – all white (no details)
 - Dark (shadow) areas – all black (no details)
- What to do?
 - Adjust exposure (time, aperture, sensitivity) to get the most important stuff
 - Acquire “High Dynamic Range” Imagery
 - Special sensors
 - Multiple exposures (at different settings) – cool thing to do
 - HDR later in the course

Perception of intensity

- Eye senses relative differences
 - Equivalent differences 50:100 20:40
 - Hard to tell absolute differences directly
 - Adaptation to current setting
- Can sense 1% differences
- At any given time 100:1 contrast ratio
- How many levels can you see in an image?
 - $1.01^{463} = 100.2$ (e.g. 463 1% differences = 100:1)
 - This is about 8 bits of precision (less than 9)
 - But its VERY non linear 1, 1.01, ..., 99.2, 100.2

Non-linearity of intensity



- Non-linear mapping from “amount of light” to perceived brightness
- Want uniform mapping of intensities -> perception
 - Level 1, 2, 3, ... 255 -> 1, 1.01, 1.02, ... 99, 100
- Worse: displays are non-linear too
 - Voltage -> amount of light is non-linear
 - Different displays are different
- Want to linearize the system
 - Intensity levels map nicely to perceived levels

Gamma correction



- Idea: put a non-linear function between intensity and output
 - Done as the last step (usually) – after all computations
- Could create arbitrary functions for mapping
 - Too cumbersome
- Exponential is a good approximate model
 - Exponential non-linearity of perception
 - Exponential power laws in CRTs

Modeling a display device



- 5/2 power law (five-halves)
 - Models physics of a CRT
 - Real CRTs are close, LCDs designed to be similar
- $L = M (i+\epsilon)^\gamma$
 - i = input intensity value
 - L = amount of light
 - ϵ = since zero isn't really black
 - M = maximum intensity
 - γ = specific property of display

Linearizing the display



- Define a function g that corrects for non-linearity
- $L = M (g(i))^\gamma$ (ignoring ϵ)
 - $G = 1/\gamma$
- Where do we get γ from?
 - Pick it so things look right
- Note: 1st order approximation (very simple)
 - Only 1 parameter to specify (γ), many factors

Gamma correction



- Want value 0 = minimum intensity
- Want value max (1 or 255) = maximum intensity
 - those 2 are easy to get
- Pick one more point
 - Midpoint should be 50%
 - Easy – show 50% black white + 50% gray
 - Adjust gamma until it looks the same
- All this happens “behind the scenes”
- Everything gets harder when we deal with color

What to store in the frame buffer?



- Frame Buffer = rectangular chunk of memory
- Intensity measurements
 - Deal with color later, basically store multiple monochrome
- Continuous range of intensities
 - 8-9 bits of precision ideally
 - More since can't get exactly right (10-12 bits)
 - More since want more dynamic range (12-14 bits)
 - More since want linear space to make math easy (16-32 bits)
- Discrete set of choices – **QUANTIZATION**
 - Inks, palettes, color tables, ...
 - Less storage cost + Color table animation

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Raster Scanning



- 2D rectangular grid (common, easy, ...)
- Serialize (1,1) (1,2) (1,3) ... (1,w), (2,1), ...
- Useful for storing in memory
- Useful for transmission
 - Send samples in order

How (analog) TV works



- CRT beam lights up phosphors
- Scans across (zig-zag pattern)
 - Horizontal, vertical retrace time
- Send images as a signal
 - Rows easy (although band-limited)
- 1930s radio technology limited rate
 - Couldn't achieve 60hz full image
 - Interlace (avoid flicker, but get full resolution)

What is a pixel



- One of these finite measurements
- At a particular position
- Point sample – value at a specific place
 - Infinitesimally small place
- Finite region of constant value (little square)
 - Doesn't actually model things better (inconsistent)
 - Mathematically less convenient
 - Useful for some thought experiments later on

A pixel is not a little square!



- Sensors average over region
 - Doesn't mean its really peicewise constant
 - Don't really know what went on in the square
- Point Samples (paradoxically) fit better with the finite case (the buckets, screen dots)
 - Sensing – estimation of what happens at the point from the neighborhood
 - Display – neighborhood is created based on the points inside of it (splats, bleeding, ...)

Dealing with discretization



- Sampling
 - Understand what information we are throwing away
- Reconstruction
 - Recreate as well as possible from the samples
- Re-Sampling
 - Sample a sampled image
 - Transform the image
- Signal Processing / Image Processing
- Consider the 1D case first since its easier

Point Sampling Has Problems



- Miss small things
- Problem: discretization throws away information
- Don't know what happens between samples
- Sampling loses information – you cannot get back the information once its lost!

Aliasing



- Technical term for sampling problems
- If you lose information and “make it up” wrong, you get weird effects

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Dealing with discretization



- Sampling
 - Understand what information we are throwing away
- Reconstruction
 - Recreate as well as possible from the samples
- Re-Sampling
 - Use a sensor on a sampled representation
 - Transform the image
- Signal Processing / Image Processing
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